6-8-2001

Ex Ante Costs of Violating Absolute Priority in Bankruptcy

Lucian Bebchuk
Harvard Law School

Follow this and additional works at: http://lsr.nellco.org/harvard_olin

Part of the Law and Economics Commons

Recommended Citation
http://lsr.nellco.org/harvard_olin/328

This Article is brought to you for free and open access by the Harvard Law School at NELLCO Legal Scholarship Repository. It has been accepted for inclusion in Harvard Law School John M. Olin Center for Law, Economics and Business Discussion Paper Series by an authorized administrator of NELLCO Legal Scholarship Repository. For more information, please contact tracy.thompson@nellco.org.
EX ANTE COSTS OF VIOLATING
ABSOLUTE PRIORITY IN BANKRUPTCY

Lucian Arye Bebchuk

Discussion Paper No. 328
06/2001

Harvard Law School
Cambridge, MA  02138

The Center for Law, Economics, and Business is supported by a grant from the John M. Olin Foundation.

This paper can be downloaded without charge from:

The Harvard John M. Olin Discussion Paper Series:
http://www.law.harvard.edu/programs/olin_center/
Ex Ante Costs of Violating Absolute Priority in Bankruptcy

Lucian Arye Bebchuk

Abstract

A basic question for the design of bankruptcy law concerns whether value should be divided in accordance with absolute priority. Research done in the past decade has suggested that deviations from absolute priority have beneficial *ex ante* effects. In contrast, this paper shows that *ex post* deviations from absolute priority also have negative effects on *ex ante* decisions taken by shareholders. Such deviations aggravate the moral hazard problem with respect to project choice -- increasing the equityholders' incentive to favor risky projects -- as well as with respect to borrowing and dividend decisions.

JEL classification: G33, K20, K22
Key words: Bankruptcy, Chapter 11, corporate reorganizations, workouts, absolute priority, moral hazard, asset dilution, claim dilution,

Copyright 2001 Lucian Arye Bebchuk. All rights reserved.
The bankruptcy rules of the United States often enable the equityholders of companies in financial distress to extract deviations from absolute priority (AP) – that is, obtain some value even when the debtholders are not paid in full. One important way in which the equityholders can do so is by putting (or threatening to put) the company in Chapter 11 (Ch. 11) of the Bankruptcy Code. Once Ch. 11 is commenced, there is an "automatic stay" which prevents debtholders from getting any value until a reorganization plan is adopted. The equityholders can use their power to prevent or delay the adoption of a reorganization plan in order to extract deviations from AP. Indeed, there is a large body of empirical work documenting that significant deviations from AP are common in Ch. 11 reorganizations. Furthermore, having the threat to put the company into Ch. 11 also strengthens the ability of equityholders to extract deviations from AP in “workouts” negotiated outside a formal bankruptcy. The deviations from AP under Ch. 11, it should be stressed, arise from the structure of its rules. The rules of Chapter 7 of the Bankruptcy Code, and the rules governing receiverships in the U.K., generally produce a division of value that is consistent with AP.

While the distributive consequences of alternative bankruptcy rules are by themselves irrelevant for efficiency, the substantial interest in them by financial economists reflects the recognition that such consequences might have significant ex ante efficiency effects. Economists have devoted much attention to analyzing optimal bankruptcy procedures and bankruptcy reform. It is generally recognized that one important goal for bankruptcy is attaining an optimal division of bankruptcy value (see, e.g., Hart (1995)

---

1 See Bebchuk and Chang (1992) for a bargaining model that identifies the sources of the equityholders' power to extract value from debtholders.


3 For a theoretical analysis of how the availability of Ch. 11 shapes the bargaining in workouts outside bankruptcy, see Brown (1989), White (1989), and Berkovitch and Israel (1998). For empirical studies of such workouts, and of the concessions made in them by debtholders, see Gilson, John, and Lang (1990), and Franks and Torous (1992, 1994).

4 For a comparison of U.S. and U.K. law, see Franks, Nybourg, and Torous (1996).
The \textit{ex post} division that is optimal is the one that would have the best overall effect on \textit{ex ante} incentives and behavior.

Much of the research on bankruptcy procedures and reform (though, as noted below, not all of it) has assumed that AP is the optimal division and has focused on procedures that could secure AP. One approach that could attain AP and that has received substantial attention is that of conducting an auction (see Baird (1986), Jensen (1991), Bhattacharyya and Singh (1999), and Rhodes-Kropf and Viswanathan (2000)). Another approach that could attain AP is based on the use of options (see Bebchuk (1988), Aghion, Hart, and Moore (1992), and Bebchuk (2000, 2001)). As noted, to identify the \textit{ex post} division of value that is optimal, it is necessary to analyze fully the \textit{ex ante} effects that this division has. Some substantial research has already been done, and it has generally suggested that the \textit{ex ante} effects of deviations from AP are actually beneficial. In particular, this line of research has shown that deviations from AP encourage desirable \textit{ex ante} investments in firm-specific human capital (Berkovitch, Israel, and Zender (1997, 1998)); that they facilitate the transfer of information to creditors and improve the timing of decisions to file for bankruptcy, to liquidate, or to recapitalize (Baird (1991)), Heinkel and Zechner (1993), Povel (1996), and Berkovitch and Israel (1998, 1999)); that they discourage excessive risk-taking by financially distressed firms (Eberhart and Senbet (1993) and Gertner and Scharfstein (1991)); and that they help address an under-investment problem in financially distressed firms with debt overhang (Berkovitch and Israel (1998), Gertner and Scharfstein (1991)), and White (1989)).

The above line of research suggests that the substantial work seeking to design procedures that would attain AP is at least unwarranted if not misguided. It also suggests that the rules of Ch. 7 and the rules of U.K. receiverships should be reconsidered. This line of research has already had an impact on the ongoing work on bankruptcy procedures and reforms. It has led to proposals to adopt procedures aimed at producing certain deviations from AP (see, e.g., Berkovitch, Israel, and Zender (1998)).

\footnote{The other widely recognized goal of bankruptcy procedures is maximizing the \textit{ex post} value of assets. This goal includes the objective of reducing the costs of the bankruptcy process (the evidence on the size of these costs is mixed, see, e.g., Cutler and Summers (1988), Lang and Stulz (1992), Warner (1977)) and the objective of ensuring an \textit{ex post} efficient allocation of the assets.}
Indeed, this research has even forced researchers who earlier put forth mechanisms aimed at attaining AP to examine how their mechanisms could be adjusted to produce distributions deviating from AP (Bebchuk (1999)).

This paper shows that *ex post* deviations from AP also have *ex ante* effects that are negative. Such deviations have an adverse effect on *ex ante* management decisions made prior to the onset of financial distress. In the presence of debt, equityholders might make "inefficient" management decisions concerning investment, distribution of dividends, and financing (see Jensen and Meckling (1976)). As will be shown, the presence of AP violations aggravates this moral hazard problem and increases its efficiency costs.

In particular, deviations from AP increase the bias of equityholders' decisions in favor of riskier investments (Jensen and Meckling (1976), Green (1984)). Equityholders (and managers seeking to maximize the value of equity) might favor a risky project over a safer one even if the risky project offers a somewhat lower expected return, because the returns from favorable outcomes of the risky project would be captured by the equityholders, whereas the losses from its unfavorable outcomes would be partly borne by the debtholders. As this paper shows, *ex post* deviations from AP produced by Ch. 11 or otherwise strengthen this distortion in favor of risky projects.

The intuition underlying this result is that AP violations operate to increase what the equityholders would receive in bad times and thus the fraction of the downward risk that would be borne by the debtholders. This increase aggravates the distortion in favor of risky projects, because it is the prospect of shifting downward risk to debtholders that creates this distortion. Moreover, the introduction of AP violations increases the nominal interest rate (to compensate the debtholders for getting less in bad times), and this increase in the nominal rate worsens further the distortion in favor of risky projects, because such an increase lowers the attractiveness of safe projects more than it lowers the attractiveness of risky projects. (With a risky project, the likelihood that the increased nominal rate would actually be paid is smaller than with a safe project.)

While the model focuses on how AP violations aggravate the extent to which choices among projects are distorted by moral hazard, the model's logic also applies to other management decisions –
such as those concerning the distribution of dividends and the taking of extra debt – that are subject to moral hazard. Deviations from AP strengthen the moral hazard problem also with respect to such decisions.

The analysis is organized as follows. Section I presents the framework of analysis. Section II analyzes *ex ante* behavior and share value in a regime without deviations from AP. Section III analyzes behavior and share value in the presence of such deviations. Section IV discusses the generality of the model’s results. Finally, Section V concludes.

I. The Model

The sequence of events in the model is as follows. At time $t = 0$, a company borrows an amount $D > 0$. At time $t = 1$, the equityholders will make a choice between two projects (or business strategies) in which the firm’s assets (including the borrowed funds) can be deployed: one is "safe," the other is "risky." Finally, at time $t = 2$, the firm’s final output $W$ is realized, and this output is divided between the equityholders and the debtholders.

A. The Initial Debt Contract

It is assumed for simplicity that all participants are risk-neutral. Let $i$ denote the interest rate set by the participants at $t = 0$ for the period between the raising and payment of debt; that is, at $t = 2$ the company will owe its debtholders the amount $D(1+i)$. Let $i_0$ denote the corresponding riskless interest rate. Given risk neutrality, the parties must choose $i$ such that the expected return to the debtholders is at least $i_0$. We assume that potential debtholders compete to offer the interest rate $i$ most favorable to the equityholders, subject to the debtholders’ "individual rationality" constraint that the expected payment to the debtholders is at least $D(1+i_0)$.

B. The Management Decision

At $t=1$, the management decision of project choice is made. We assume that this management
decision is made by the equityholders – or, equivalently, by managers seeking to serve the interests of the equityholders (at least as far as the considered management decision is concerned). We also assume that the equityholders’ choice of project is not verifiable, so that it cannot be specified in the initial debt contract.

If the equityholders choose the "safe" project, then the final output $W$ will be $S$, where $S > D(1+i)$. If they choose the risky project instead, then the final output $W$ will be $\theta R$, where $R$ is the expected return, which is positive, and $\theta$ is a random variable with expected value equal to 1. Let $\theta$ be distributed continuously with positive density throughout the interval $(0, \theta)$, where $\theta > 1$. At $t = 1$, the equityholders observe $R$, but the value $\theta$ is realized at $t = 2$.

At $t = 0$, all the participants know that at $t = 1$, the equityholders will choose between a safe project and a risky project. Not all the details of this choice, however, are known in advance. It is assumed that given the information available at $t = 0$, the parties know $S$ but only the distribution of $R$. The risky project may offer a higher or lower expected return than the safe project. Specifically, let $R$ be distributed continuously with positive density throughout the interval $(0, R)$, where $R > S$. The moral hazard problem is that at $t = 1$ the equityholders may choose the risky project even if $R < S$.

C. The Final Period

At $t = 2$, the final output $W$ is realized and then divided between the equityholders and the debtholders. This division depends upon whether the option of filing for Ch. 11 is available. As explained earlier, the availability of Ch. 11 substantially increases the equityholders’ power to extract deviations from AP. We assume that such deviations are possible only with Ch. 11.

Thus, under the regime in which Ch. 11 is not available, the equityholders will not be able to extract concessions from the debtholders. If the firm is insolvent, $W < D(1+i)$, then its assets will be sold as a going concern through a Ch. 7 liquidation, and the proceeds will be applied first to cover the firm's debt. Thus, under this regime, the equityholders will receive $\max[W - D(1+i), 0]$, and the debtholders will receive $\min[D(1+i), W]$. 

5
In contrast, under the Ch. 11 regime, the equityholders will be able to obtain some value regardless of how small W turns out to be. Specifically, if $W < D(1+i)$, the shareholders, by filing for Ch. 11 or threatening to do so, will be able to obtain $\alpha W$ (where $\alpha > 0$).\(^6\) Moreover, the equityholders, by using or threatening to use Ch. 11, will be able to obtain more than their contractual right if the firm is sufficiently close to "insolvency" – that is, if $W$ exceeds $D(1+i)$ by an amount that is sufficiently small.\(^7\) For simplicity, it will be assumed that the equityholders will always be able to get at least $\alpha W$ even if their "contractual right" of $W - D(1+i)$ is less than that. That is, if $0 < W - D(1+i) < \alpha W$, the equityholders will get $\alpha W$ while the debtholders will not get full payment but only $(1-\alpha)W < D(1+i)$. Thus, under the Ch. 11 regime, the equityholders will receive $\max[ W - D(1+i), \alpha W ]$, and the debtholders will receive $\min[ D(1+i), (1-\alpha)W ]$. The assumption that the payoff to the equity in the event of insolvency will be a fixed fraction $\alpha$ of the value is made only for simplicity of notation; the results of the paper hold as long as the equityholders are able to get some value in the event that $W < D(1+i)$.

D. The Initial Equity Value

Let $V_0$ be the ex ante value of the equity, that is, the expected value of the equity at $t = 0$. The question to be addressed is whether $V_0$ is higher with or without Ch. 11. The debtholders in this model cannot be "cheated" by Ch. 11 – they will always capture an expected return $i$. Therefore, the question of which regime implies a higher $V_0$ is equivalent to the question of which regime leads to more efficient

\(^6\) Bebchuk and Chang (1992) model the bargaining process in Ch. 11 and analyze how the fraction of value that the equityholders can obtain depends on the characteristics of the firm in Ch. 11 and on the legal rules of Ch. 11. For our purposes, which are to understand how the ability to extract some value affects certain ex ante decisions, it seems appropriate to use a simple, reduced-form representation of the outcome in the Ch. 11 bargaining.

It should be noted that an assumption made later on is that $\alpha < \left[ \frac{S - D(1+i)}{S} \right]$. This assumption will be made to simplify the analysis by ensuring that only the risky project (but not the safe project) may lead to bankruptcy.

\(^7\) See Bebchuk and Chang (1992) for an analysis of how Ch. 11 can enable equityholders to obtain more than their contractual right in situations of "near-insolvency."
management decisions.

Let \( V_0^* \) denote the first-best value for \( V_0 \). Then:

\[
V_0^* = \left[ \Pr(R \neq S) \right] S + \left[ \Pr(R > S) \right] E[R^*R > S] - D(1+i).
\] (1)

As will be shown, however, this first-best value cannot be obtained under either regime.

II. No Violations of Absolute Priority

Let us start with the regime in which Ch. 11 is not available and value is distributed according to AP. We will analyze the outcome under this regime in three steps: (1) Given any agreement between the parties on the value of \( i \), how would the equityholders decide at \( t = 1 \) between the projects? (2) Given the expected management decision by equityholders, what \( i \) would be chosen \textit{ex ante} at \( t = 0 \)?, and (3) Given that particular \( i \), what project would the equityholders choose, and what \( V_0 \) would that choice imply?

A. The Equityholders’ Choice Given an Interest Rate

First consider the choice of a project at \( t = 1 \) under a regime without Ch. 11 and AP violations. Given \( i \), once the equityholders observe \( R \), they will choose the risky project if and only if:

\[
E_{\theta} \max[ \theta R - D(1+i), 0 ] \neq \max[ S - D(1+i), 0 ].
\] (2)

Let \( R_0(i) \) denote the smallest nonnegative value of \( R \) that makes the left- and right-hand sides of (2) equal. There always exists such a value. The equityholders will choose the risky project if and only if \( R \neq R_0(i) \).

Using Jensen’s inequality and the convexity of the max function in (2), one can show that if a risky project with \( R = S \) does not always lead to insolvency, that is, \( \theta S > D(1+i) \), then the left-hand side of (2) is strictly greater than its right-hand side for \( R = S \). Furthermore, if \( D(1+i) \neq S \), then the right-hand side of (2) equals 0, and \( R_0(i) = 0 \). It follows that for any given \( i \):

\[
R_0(i) < S.
\] (3)
Inequality (3) implies that the equityholders may choose the risky project even if $R < S$. This result is the familiar moral hazard problem (see, e.g., Jensen and Meckling (1976)). The equityholders may choose the risky project inefficiently, because they have more to gain from a favorable outcome for this project than they have to lose from an unfavorable outcome.

B. The Equilibrium Interest Rate

Let $i_N$ be the interest rate set by the parties at $t = 0$ under the no-reorganization regime. Let $F_N(i)$ be the expected payment to debtholders for any given $i$ under the regime with no Ch. 11 and AP violations. Thus:

$$F_N(i) = \Pr[ R < R_N(i) ] \min[ D(1+i), S ] +$$

$$\Pr[ R \geq R_N(i) ] E_R\{ E_{\min[ D(1+i), \theta R R_N(i) ]} \}. \quad (4)$$

Let us assume that there exists some $i$ that satisfies the debtholders' constraint, $F_N(i) \geq D(1+i_0)$, and provides the equityholders with a positive expected value. In a competitive market for debt, the equilibrium interest rate $i_N$ will satisfy:

$$F_N(i_N) = D(1+i_0). \quad (5)$$

Note our assumption that there exists such an $i_N$ that leaves the equityholders with a positive expected value implies that this $i_N$ allows some positive probability of solvency. Thus, $i_N$ satisfies $D(1+i_N) < \theta R$, or $i_N < (\theta R / D) - 1$.

C. The Initial Value

Let $V_0^N$ be the *ex ante* value of the equity under the no-reorganization regime. As (5) reveals,  

---

8 If the moral hazard problem is sufficiently severe, such an $i$ might not exist. In such a case, the moral hazard problem would prevent the firm from borrowing the amount $D$.  

---
the debtholders in this case capture an expected return \( i_0 \). Therefore:

\[
V_0^N = \Pr[ R < R_N(\bar{i}_N)] S + \Pr[ R \geq R_N(\bar{i}_N)] E[ R^* R \geq R_N(\bar{i}_N)] - D(1+i_0).
\]

Note that since \( R_N(\bar{i}_N) < S \) (see (3)), the \( V_0^N \) in (6) falls short of the first-best value \( V_0^* \) in (1). Specifically, \( V_0^N \) is lower than \( V_0^* \) by the difference: \( \Pr[ R_N(\bar{i}_N) \not< R < S] E[ S-R^* R_N(\bar{i}_N) \not< R < S] \).

III. Violations of Absolute Priority

We now turn to analyze the reorganization regime in which CH. 11 is available and deviations from AP occur. We will follow the same three steps as in the preceding analysis of the no-reorganization regime. Accordingly we start with the question of how the equityholders will choose between the projects given an interest rate.

A. The Equityholders' Choice Given an Interest Rate

Consider the choice of a project at \( t = 1 \) under a regime with Ch. 11. Given \( i \), once the equityholders observe \( R \), they will choose the risky project if and only if:

\[
E_\theta \max[ \theta R-D(1+i), \alpha \theta R ] \leq \max[ S-D(1+i), \alpha S ].
\]

Let \( R_R(i) \) denote the unique value of \( R \) that makes the left- and right-hand sides of (7) equal. There always exists such a value. The equityholders will choose the risky project if and only if \( R \leq R_R(i) \).

We can now compare the project choices at \( t = 1 \) under the two regimes for any given \( i \). As the following proposition indicates, for any given \( i \#[ S(1-\alpha)/D ] - 1 \), the availability of Ch. 11 makes the equityholders more likely to choose the risky project.

**Proposition 1:** \( R_R(i) < R_N(i) \), for any \( i \#[ S(1-\alpha)/D ] - 1 \).

**Remark:** The intuition behind this result (which is proved in the Appendix) is as follows. Under both

---

9 Under this condition concerning \( i \), only the risky project, but not the safe project, may lead to corporate reorganization.
regimes, the equityholders have an inefficient incentive to invest in risky projects. The availability of Ch. 11, however, increases this incentive (holding fixed the interest rate) because it increases the attractiveness of a risky project for the equityholders. Under both regimes, the equityholders capture the benefits of a favorable outcome from the risky project, whereas the debtholders bear part of the costs of an unfavorable outcome. With Ch. 11, however, the debtholders bear a larger fraction (and the equityholders bear a smaller fraction) of the downside risk, which makes the risky project more attractive for the equityholders (relative to the situation without Ch. 11). Thus, the presence of Ch. 11 enhances the severity of the moral hazard problem.

B. The Equilibrium Interest Rate

Let $i_R$ be the interest rates set by the parties at $t = 0$ under the reorganization regime. Let $F_R(i)$ be the expected payment to debtholders for any given $i$ under the reorganization regime. Thus:

$$F_R(i) = \Pr[ R < R_R(i) ] \min[ D(1+i), S(1-\alpha) ] +$$

$$\Pr[ R \leq R_R(i) ] E_{R_R} \{ E_{\theta} \min[ D(1+i), \theta R(1-\alpha) ] + R_R(i) \}. \quad (8)$$

Let us assume that there exists some $i$ that satisfies the debtholders' individual nationality constraint, $F_R(i) \leq D(1+i_0)$. In the competitive debt market, $i_R$ will satisfy:

$$F_R(i_R) = D(1+i_R). \quad (9)$$

Let us also assume that $S(1-\alpha)/D$ is large enough to ensure that the debtholders' constraint can be satisfied by some $i \# [ S(1-\alpha)/D ] - 1$, so that $i_R \# [ S(1-\alpha)/D ] - 1$. This assumption implies that $i_R$ is small enough to ensure that the safe project will not lead to Ch. 11 (only a risky project will).

Proposition 2: The equilibrium interest rate is higher under the reorganization regime with AP violations than under the no-reorganization regime: $i_R > i_N$.

---

10 Again, if the moral hazard problem is sufficiently severe, such an $i$ might not exist, in which case the moral hazard problem would prevent the firm from borrowing the amount $D$. 
Remark: The proof of the proposition is in the Appendix, but its intuition might be briefly described as follows. Introducing violations of AP while maintaining the interest rate \( i_N \) would hurt the debtholders for two reasons. First, the equityholders would be more inclined to choose a risky project (Proposition 1). Second, the debtholders would expect to get a smaller fraction of the final output in the event of insolvency or financial distress. For both reasons, introducing AP violations while keeping \( i_N \) would give the debtholders less than competitive returns. Therefore, a higher interest rate than \( i_N \) will be necessary to offer the debtholders the same competitive expected return \( D(1+i_0) \).

C. The Initial Value

Let us now consider the initial equity value under the reorganization regime and compare it to the value under the no-reorganization regime. Let \( V_0^R \) denote the *ex ante* value of the equity under the reorganization regime. As (9) reveals, the debtholders capture an expected return \( i_R \), and thus:

\[
V_0^R = \Pr[ R < R_R(i_R) ] \cdot S + \Pr[ R \geq R_R(i_R) ] \cdot E[ R^* R_R(i_R) ] - D(1+i_0). \tag{10}
\]

Note that since \( R_R(i_R) < S \) (see (8)), \( V_0^R \) in (10) falls short of the first-best value \( V_0^* \) in (1) by the difference: \( \Pr[ R_R(i_R) \# R \# S ] \cdot E[ S - R^* R_R(i_R) \# R \# S ] \).

The initial value again depends upon the expected investment decisions given the equilibrium interest rate. Thus, to compare \( V_0^R \) and \( V_0^N \), we must begin with a comparison of \( R_R(i_R) \) and \( R_N(i_N) \).

**Proposition 3:** The likelihood that a risky project will be chosen is greater under the reorganization regime than under the no-reorganization regime: \( R_R(i_R) < R_N(i_N) \).

Remark: This result, which is proved in the Appendix, can be intuitively explained as follows. The availability of Ch. 11 aggravates the moral hazard problem for two reasons. First, with Ch. 11, equityholders are more inclined to choose the risky project, because Ch. 11 shifts more downside risk from the equityholders to the debtholders. Second, the equilibrium interest rate is higher under the reorganization regime – and this further reduces the attractiveness of the safe project compared to the risky project.
Our result, that the moral hazard problem is more severe if Ch. 11 is available, leads us, by straightforward algebra, to the following conclusion.

**Proposition 4:** The initial equity value is lower under the reorganization regime than under the no-reorganization regime by the difference:

$$\Pr[ R_R(k_R) # R < R_N(k_N) ] E[ S - R^* R_R(k_R) # R < R_N(k_N) ].$$  \hspace{1cm} (11)

The equityholders bear the cost of any inefficient behavior, because the debtholders take the *ex post* opportunism of equityholders into account *ex ante*. More inefficient project choices are expected under the reorganization regime (Proposition 3). Therefore, $V_0^R$ is lower than $V_0^N$ by the cost of the additional inefficient project choices.

**D. Note on Magnitude**

The magnitude of the efficiency costs of the AP violations – the extra moral hazard costs that such violations produce – is given by (11) above. And future research might wish to examine, both theoretically and empirically, the magnitude of these extra costs.

As emphasized earlier, the identified distortion exacerbates the moral hazard problem that would arise even without AP violations from the mere presence of limited liability. Even without AP violations, the presence of limited liability implies that the adoption of a risky project would impose a negative externality on existing debt, or, in other words, would force the debt to provide a “subsidy” to the equity. The introduction of AP violations provides extra “subsidy.” Since debtholders commonly lose a substantial amount in bankruptcy even in the absence of AP violations, and AP violations are commonly limited to only a fraction of the bankruptcy value, it might be suggested that the extra subsidy might not be large relative to the basic subsidy arising from the mere presence of limited liability.\(^{11}\)

\(^{11}\)I am grateful to an anonymous referee for raising this question. The referee motivated this skeptical question by estimating the relative increase in the size of the subsidy using some of the empirical evidence on the average recovery in bankruptcy and the average size of deviations from AP. Assuming that the average reorganization value is half of the value of the outstanding debt, and that the deviations from absolute priority average 10 percent of the reorganization value, the referee calculated that the deviations
Note, however, that the relative increase in the size of moral hazard costs produced by AP violations might be larger than the relative increase in the subsidy produced by them. The reason for this is that the marginal inefficient risky projects that would be induced if AP violations were added on top of limited liability are more inefficient than the inefficient risky projects that would be adopted under limited liability alone. That is, one should not equate the relative increase in moral hazard costs produced by AP deviations with the relative increase in the size of the subsidy produced by them. To estimate the relative increase in moral hazard costs, a more complex analysis would be needed, which would, among other things, have to estimate (or make an assumption about) the distribution of inefficient risky projects.

Furthermore, note that the same skeptical observation can also be made about the magnitude of the beneficial effects of AP violations identified by other \textit{ex ante} models of the effects of such violations. As was emphasized, a main point of this paper is that, unlike what one might otherwise infer from the literature modeling the \textit{ex ante} effects of AP violations, such violations are not unambiguously beneficial. In the other existing models, the beneficial effects of AP violations result from the fact that the subsidy to equity provides equityholders with incentives to take certain beneficial \textit{ex ante} actions. To the extent that this subsidy is not large, questions also arise about the magnitude of the beneficial effects identified by these other models. Thus, while questions regarding the size of the subsidy under the existing AP violations might raise doubts concerning whether the \textit{ex ante} effects of these violations are important, they do not resolve the question of whether these violations are overall positive or negative, and thus do not undermine this paper’s main point, that these violations might overall be undesirable.

IV. Other Ex Ante Decisions

\textbf{A. Project Choice after the Onset of Financial Distress}

Let us now reconcile the result obtained above with the results in other papers that deviations from AP can have a beneficial effect on management decisions once the firm is in financial distress. Observe that a critical assumption in the preceding analysis was that the safe project, the one that from AP would increase the average subsidy to equity by only 10 percent.
involves less output volatility, is associated with lower likelihood of insolvency. This assumption is likely to hold for most companies that are safely distant from financial distress. Once the fortunes of a firm deteriorate, however, it might reach a situation in which a safe investment policy would produce a greater likelihood of insolvency than would a riskier policy. In such situations, which are common in financial distress, Ch. 11 might well operate to reduce the moral hazard distortion in favor of risky projects.

Consider a situation in which the safe project's return is $S < D(1+i)$. In this case, if the safe project is chosen, the company will surely reach insolvency. Consequently, if Ch. 11 is not available, the distortion would be substantial – the equityholders have nothing to lose and something to gain from choosing a risky project; therefore, they will choose any risky project, whatever its expected return, as long as it offers some chance of solvency. In contrast, with Ch. 11, the equityholders can expect to get something in the event of insolvency, and it is thus no longer the case that they have nothing to lose if they choose a risky project with a very low expected return. Consequently, they will now choose the risky project only if its expected return exceeds a certain threshold. Thus, consistent with the results of other papers (see Eberhart and Senbet (1993) and Gertner and Scharfstein (1991)), when the firm is already in financial distress, Ch. 11 would have the positive effect of reducing moral hazard.

B. Decisions concerning Distributions and Borrowing

The model suggests that Ch. 11 affects not only ex ante choices between safe and risky projects but also other ex ante management decisions. In addition to the "asset substitution" problem concerning project choice, the presence of debt also creates problems of "asset dilution" and "claim dilution" (Smith and Warner (1979)). The asset dilution problem concerns decisions about distributions to equityholders – the equityholders have an incentive to take an excessive value out of the firm (say, in the form of dividends or salaries). The claim dilution problem concerns decisions to take extra debt when some debt is already in place – the equityholders have an incentive to take an excessive amount of additional debt.
The presence of Ch. 11 can be shown to aggravate the problems of asset dilution and claim dilution for exactly the same reason that it aggravates the asset substitution problem. In the presence of debt, equityholders will tend to withdraw too many assets and take too much extra debt because, in the event of insolvency, some of the costs resulting from such actions would fall upon debtholders. The presence of Ch. 11 increases the fraction of the loss borne by the debtholders in the event of insolvency — and, as a result, it strengthens these inclinations and thereby exacerbates the problems of asset dilution and claim dilution.

V. Conclusion

Much research on bankruptcy procedures and reform has focused on designing procedures that would eliminate deviations from AP. Consistent with the view underlying this line of research, this paper has shown that deviations from AP have an adverse *ex ante* effect on management decisions. Such deviations exacerbate the problems of asset substitution, asset dilution, and claim dilution.

One possible way to test this model would be to examine how the adoption of Ch. 11 in 1978 affected the use of covenants. The 1978 reform greatly increased the ability of equityholders to extract value in the event of insolvency or financial distress. The implication of the model is that, because the 1978 reforms exacerbated the problem of moral hazard, they should have led to more extensive use of covenants in order to discourage asset substitution, asset dilution, and claim dilution.

To be sure, to determine whether deviations from AP are overall undesirable, it would be necessary to compare the magnitude of their negative effect, which this paper analyzes, with the magnitude of those positive effects of such deviations, which other papers have identified. One casual observation that is consistent with the view that AP is overall desirable is that, in countries like the U.K. in which insolvency law does not produce significant deviations from AP, parties do not generally provide for such deviations in their contracts. The question whether the total *ex ante* effect of such deviations is positive or negative is one that would be important for future work to pursue.
APPENDIX

Proof of Proposition 1: For any i satisfying the condition of the proposition, the right-hand sides of (2) and (7) are equal (because choosing the safe project would never result in the equityholders' using Ch. 11). Recall that \( \theta \) can be arbitrarily close to 0 with some positive probability, which implies:

\[
0 < \Pr[ D(1+i) > \theta R(1-\alpha) ] = \Pr[ \alpha \theta R > \theta R - D(1+i) ].
\] (A1)

Therefore, the left-hand side of (7) is strictly greater than the left-hand side of (2). Furthermore, if \( R = R_N(i) \), then the left-hand side of (2) is equal to the right-hand side of (2), which is equal to the right-hand side of (7). To make (7) an equality then, R must fall below that level: \( R_R(i) < R_N(i) \). Q.E.D.

Proof of Proposition 2: Recall that \( i_N \) will be the smallest value meeting the constraint that the debtholders are offered no less than a competitive return, which by (5) will be binding. Thus, any smaller i must fail to satisfy the relevant constraint:

\[
F_N(i) < F_N(i_N), \quad \text{úi} < i_N.
\] (A2)

Therefore, if we suppose, contrary to the proposition, that \( i_R \neq i_N \), then:

\[
F_N(i_R) \neq F_N(i_N).
\] (A3)

Furthermore, because \( i_R \) satisfies \( D(1+i) \neq S(1-\alpha) \), a comparison of (4) and (8) reveals that:

\[
F_R(i_R) < F_N(i_R).
\] (A4)

Together, (A3) and (A4) imply that \( F_R(i_R) < F_N(i_N) \), which contradicts the implication of (5) and (9) that

\[
F_R(i_R) = F_N(i_N).
\] Q.E.D.

Proof of Proposition 3: First, it will be useful to establish the following inequality:

\[
R_N(i) < 0, \quad \text{úi} < (S/D) - 1.
\] (A5)
Note that if $D(1+i) < S$, then the right-hand side of (2) is simply $S - D(1+i)$, and $R_N(i)$ is defined by the equality:

$$E_{\text{max}}[\theta R_N - D(1+i), 0] = S - D(1+i),$$

or equivalently:

$$E_{\text{max}}[\theta R_N, D(1+i)] = S.$$  \hspace{1cm} (A6)

Note that $\theta R_N < D(1+i)$ with some positive probability, because by assumption, $\theta$ can be arbitrarily close to 0 with some positive probability. Therefore, the left-hand side of (A6) is strictly increasing in $i$.

Note also that $\theta R_N > D(1+i)$ with some positive probability – otherwise, the equality in (A6) could not possibly hold, because $D(1+i) < S$ by assumption. Therefore, the left-hand side of (A6) is also strictly increasing in $R_N$. The right-hand side of (A6), however, is independent of both $i$ and $R_N$. Therefore, if $i$ increases, then to maintain the equality in (A6), $R_N$ must decrease, which proves (A5).

Given that $i_R$ is assumed to satisfy $D(1+i) \not\# S(1-\alpha)$, Proposition 1 implies that:

$$R_R(i_R) < R_N(i_R).$$  \hspace{1cm} (A7)

Furthermore, Proposition 2 and (A5) together imply that:

$$R_N(i_R) < R_N(i_N).$$  \hspace{1cm} (A8)

Together (A7) and (A8) yield Proposition 3.

Q.E.D.
REFERENCES


Betker, Brian, 1995, Management’s incentives, equity’s bargaining power, and deviations from absolute


